

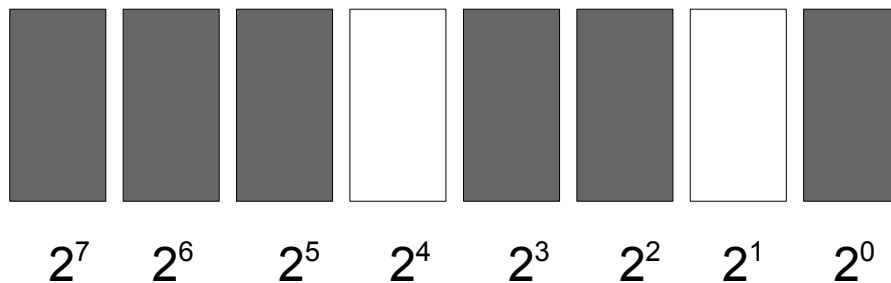
# Binary Base

# Introduction

- “A binary numeral system is a numeral system that represents numeric values using two symbols, usually 0 and 1. The binary system is used internally by all computers.” (wikipedia.org)

# Bits & Bytes

- Binary numbers can be represented via a sequence of bits (binary digits) that can be represented by any mechanism capable of being in two mutually states (e.g. small magnetic field).



# Binary & Decimal

- Converting a binary number into a decimal one is done by multiplying each one of the digits (starting with the rightmost digit representing  $2^0$ ) by  $2^n$ .

The 'n' stands for the digit position. The position of the rightmost digit is 0.

$$\begin{array}{cccccccccc} 1 & 0 & 0 & 1 & 0 & 1 & 0 & 1 & 1 & 1 \\ 2^9 & 2^8 & 2^7 & 2^6 & 2^5 & 2^4 & 2^3 & 2^2 & 2^1 & 2^0 \end{array}$$

$$1*2^9+1*2^6+1*2^4+1*2^2+1*2^1+1*2^0 = 512 +64+16+4+2+1=599$$

# Binary & Decimal

- Converting a decimal number into a binary one is done by dividing the decimal number by 2 while keeping the residual aside and continue with dividing by 2 each result we get.

$$25 / 2 = 12 \quad 1$$

$$12 / 2 = 6 \quad 0$$

$$6 / 2 = 3 \quad 0$$

$$3 / 2 = 1 \quad 1$$

$$1 / 2 = 0 \quad 1$$

$$25_{10} = 11001_2$$

# Bitwise Operations

- NOT

This is an unary operation that goes over each bit and change it into 1 (instead of 0) and into 0 (instead of 1).

NOT 01111 = 10000

NOT 10101 = 01010

In many programming languages the bitwise NOT operator is '~'.

# Bitwise Operations

- OR

This operation takes two bit patterns with the same length and produce a new one with the same length by matching each one of the bits and performing a logical inclusive OR. For each pair the result is 1 if at least one of the two bits is 1. In all other cases the result is 0.

110010 OR 111100 = 111110

101 OR 100 = 101

In many programming languages the bitwise NOT operator is '|'.

# Bitwise Operations

- AND

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110010 AND 111100 = 110000

101 OR 100 = 100

In many programming languages the AND operator is '&'.



# Bitwise Operations

- XOR

This operation takes two bit patterns with the same length and produce a new one with the same length by matching each one of the bits and performing a logical bitwise exclusive XOR operation. For each pair the result is 1 if the two bits are different. In all other cases the result is 0.

110 XOR 111 = 001

0101 OR 1100 = 1001

In many programming languages the XOR operator is '^'.

# Binary Base

12/31/08

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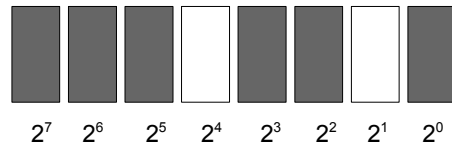
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